

ED de Variables Separables

Resolver las siguientes ecuaciones diferenciales:

1. $\frac{dy}{dx} = \tan x + \sec x$

1

2. $\frac{dy}{dx} = \tan y$

2

3. $\frac{dx}{dy} = \frac{x^2}{y}$

3

4. $\frac{dx}{dy} = \frac{y}{x^2}$

4

5. $\frac{ds}{dt} = \frac{(2t+1)(2s-1)}{2(t^2+t)}$

5

6. $\frac{ds}{dt} = \frac{(s^3-s)(4t^3-6t)}{(t^4-3t^2)(3s^2-1)}$

6

7. $\frac{du}{dt} = \frac{(u+1)(t+1)}{(u+2)(t-1)}$

7

8. $\frac{dt}{du} = \frac{tu+u+3t+3}{tu+2u-t-2}$

8

9. $x^2 y' = 1 - x^2 + y^2 - x^2 y^2$

4

10. $xy' - y = 2x^2 y$

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11. $4tx \frac{dx}{dt} = x^2 + 1$

11

12. $(y \ln x)^{-1} \frac{dy}{dx} = \left(\frac{x}{y+1} \right)^2$

12

13. $\frac{d\theta}{dt} = (\cos t)(\cos 2\theta - \cos^2 \theta)$

13

14. $\frac{dy}{dt} = e^{-2t+3y}$

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15. $\frac{dy}{dx} + y = yxe^{x+2}$

15

16. $e^x y dy - (e^{-y} + e^{2x-y}) dx = 0$

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17. $2tx^2 + 2t + (t^4 + 1)x' = 0, \text{ con } x(0) = 1$

18

18. $\frac{2r-1}{t} dr + \frac{r-2r^2}{t^2-1} dt = 0, \text{ con } r(2) = 4$

19

19. $\frac{1}{(y-1)^2} dx + \frac{1}{\sqrt{x^2+4}} dy = 0$

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20. $\frac{dT}{dt} = k(T - T_1), \text{ con } T(0) = T_0, \text{ donde } k, T_0, T_1 \text{ son constantes}$

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